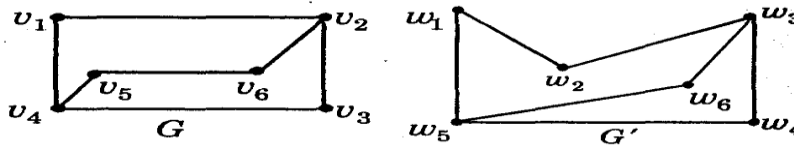


**Assignment-III**  
**MODULE-3**  
**(GRAPH THEORY)**

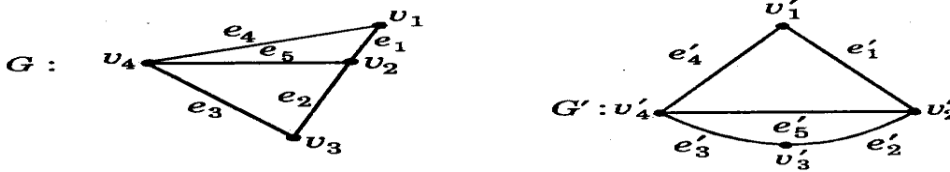
1. Prove that the minimum no. of edges in a connected graph with  $n$  vertices is  $n-1$ .
2. Suppose  $G$  is a non-directed graph with 12 edges. If  $G$  has 6 vertices each of degree 3 and rest have degree less than 3, find the minimum number of vertices in  $G$ .
3. Show that the graphs  $G$  and  $G'$  are isomorphic.



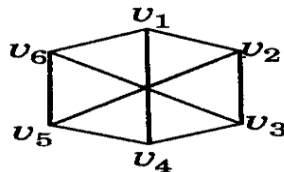
4. Draw the graph whose incidence matrix is given below

$$\begin{bmatrix} 0 & 0 & 1 & -1 & 1 \\ -1 & 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 1 & 0 & 0 & 0 & -1 \\ 0 & 1 & 0 & 0 & 0 \\ 0 & 0 & -1 & 1 & 0 \end{bmatrix}$$

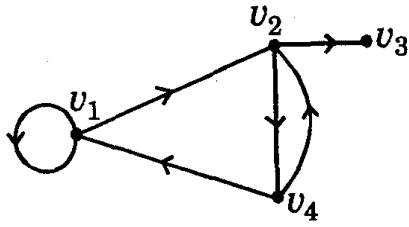
5. Prove that the maximum number of edges in a connected simple graph with  $n$  vertices is  $\frac{n(n-1)}{2}$ .
6. Examine whether the following two graphs are isomorphic.



7. Define the complement of a graph. Find the complement of the graph.



8. Construct the Adjacency matrix of the diagram.



9. Show that the maximum number of edges in a disconnected graph with  $n$  vertices and  $k$  components is  $\frac{1}{2}(n-k)(n-k+1)$ .

10. Examine whether the following two graphs are isomorphic.

