Assignment –I

MODULE-1

(ORDINARY DIFFERENTIAL EQUATION OF FIRST ORDER & FIRST DEGREE)

Solve the following differential equation by finding integrating factors:

1.
$$(y^2 + 2x^2y)dx + (2x^3 - xy)dy = 0$$

2.
$$xdy - ydx = (x^2 + y^2)(xdx + ydy)$$

3.
$$4x^3ydx + (x^4 + y^4)dy = 0$$

4.
$$(3x^2y^4 + 2xy)dx + (2x^3y^3 - x^2)dy = 0$$

5.

Solve:

1.
$$y(2x^2y + e^x)dx - (e^x + y^3)dy = 0$$

2.
$$cosx(cosx - sin \propto siny)dx + cosy(cosy - sin \propto sinx)dy = 0$$

3.
$$(1+4xy+2y^2)dx+(1+4xy+2x^2)dy=0$$

4.
$$(y^2e^{xy^2} + 4x^3)dx + (2xye^{xy^2} - 3y^2)dy = 0$$

Solve the following differential equations:

1.
$$dx + xdy = e^{-y}sec^2ydy$$

2.
$$\frac{dy}{dx} + \frac{y}{x}logy = \frac{y}{x^2}(logy)^2$$

3.
$$\frac{dy}{dx} + \frac{1}{x}tany = \frac{1}{x^2}tanysecy$$

$$4. \quad y(2xy + e^x)dx - e^x dy = 0$$

$$5. \ \frac{dy}{dx} = e^{x-y}(e^x - e^y)$$

6.
$$xy - \frac{dy}{dx} = y^3 e^{-x^2}$$

Find the general solution of the following equations:

1.
$$xp^2 + (y - x)p - y = 0$$

2.
$$p^2 - p(e^x + e^{-x}) + 1 = 0$$

3.
$$x^2p^2 + 3xyp + 2y^2 = 0$$

4.
$$p^3 + 2xp^2 - y^2p^2 - 2xy^2p = 0$$

$$5. \quad y = 2px + p^2y$$

6.
$$p^3 - 4xyp + 8y^2 = 0$$

7.
$$x^3p^2 + x^2py + a^3 = 0$$

8.
$$x = py - p^2$$

Obtain the general & singular solutions of the following differential equations:

1.
$$py = p^2(x - b) + a$$

2.
$$y = px + p - p^2$$

Obtain the general solution of the following differential equations:

$$1. \quad y = 2px + 4yp^2$$

1.
$$y = 2px + 4yp^2$$

2. $y - 2px + ayp^2 = 0$

$$3. \quad (px - y)(x - py) = 2p$$

3.
$$(px - y)(x - py) = 2p$$

4. $x^2p^2 + yp(2x + y) + y^2 = 0$